## Macroeconomic and Financial Risks: a Tale of Mean and Volatility

Dario Caldara ${ }^{1} \quad$ Chiara Scotti $^{2} \quad$ Molin Zhong $^{1}$<br>${ }^{1}$ Federal Reserve Board<br>${ }^{2}$ Federal Reserve Bank of Dallas

## June 2023 <br> 12th ECB Conference on Forecasting Techniques

## Motivation

"Therefore, the Committee's policy decisions reflect its longer-run goals, its medium-term outlook, and its assessments of the balance of risks, including risks to the financial system that could impede the attainment of the Committee's goals."
Statement on Longer-Run Goals and Monetary Policy Strategy, FOMC 01/31/23

- Evidence of risk management considerations in one-third of the FOMC monetary policy decisions between 1993 and 2008. (Evans et al., 2015)


## Introduction

- This paper investigates the drivers of uncertainty and tail risk of future economic conditions (GDP growth) and future financial conditions (corporate credit spreads) in the U.S. using a stochastic volatility VAR.
- We distinguish between shocks originating in the real economy and shocks originating in the financial sector.
- We impose sign and zero restrictions on structural coefficients to identify macroeconomic and financial shocks.


## Introduction

## The impact of macro and financial shocks on conditional distributions




- Adverse macroeconomic and financial shocks move simultaneously future GDP growth and corporate spreads.
- Shocks generate an increase in uncertainty and downside risk of future GDP growth and spreads, but small reduction in upside risk.
- Effect of macroeconomic shocks is largest within the first year, while financial shocks play a dominant role at longer horizons.


## Introduction <br> Decomposing the Effects of Shocks on Uncertainty and Tail Risk

- We estimate the model using Bayesian techniques and compute conditional distributions as in Del Negro and Schorfheide (2013).
- We use these conditional distributions to compute impulse responses of uncertainty and tail risk.
- We decompose the effects of our identified shocks into three channels:
- Volatility channel: Shocks alter the evolution of current and future volatilities of shocks.
- Estimation uncertainty channel: Parameter and state uncertainty make the effects of shocks more uncertain.
- "Higher-order" channel: Interaction between shocks and time-varying volatility beyond the direct effect of shocks on current and future volatility.


## Contribution to Literature

- Growth-at-Risk: ABG (2019), Plagborg-Moller et al. (2020).
- SV-VARs to estimate mean effects of time-varying volatility: Mumtaz and Zanetti (2013), Creal and Wu (2017), Carriero et al. (2018), Mumtaz (2018), Shin and Zhong (2018).
- Linear VARs to examine the relationship between uncertainty and the business cycle: Bloom (2009), Baker et al. (2016), LMN (2021).
- Nexus between macroeconomic and financial conditions: Bernanke et al. (1999), Gertler and Karadi (2011), Bocola (2016), Guerrieri and lacoviello (2017).


## PLAN FOR TALK

1. Econometric Framework
2. Identification Strategy
3. Effects of Shocks on Uncertainty and Tail Risk
4. Concluding Remarks

## Multivariate SV-VAR model

We use the model of Mumtaz (2018).
Level equation: Stochastic Volatility \& Volatility-in-mean

$$
\begin{gathered}
z_{t}=c+\sum_{j=1}^{P} \beta_{j} z_{t-j}+\sum_{k=1}^{K} b_{k} \tilde{h}_{t-k}+H_{t}^{1 / 2} e_{t} \\
H_{t}=\exp \left(\operatorname{diag}\left(\tilde{h}_{t}\right)\right)
\end{gathered}
$$

Volatility equation: Endogenous Volatility

$$
\tilde{h}_{t}=\alpha+\sum_{j=1}^{J} \theta_{j} \tilde{h}_{t-j}+\sum_{q=1}^{Q} d_{j} z_{t-j}+S^{1 / 2} \eta_{t}
$$

Covariance structure: Correlated level and volatility disturbances

$$
\varepsilon_{t}=\binom{e_{t}}{\eta_{t}} \sim N(0, \Sigma) ; \quad \Sigma=\left(\begin{array}{cc}
\Sigma_{\eta} & \Sigma_{\eta e}^{\prime} \\
\Sigma_{\eta e} & \Sigma_{e}
\end{array}\right)
$$

## Model Specification and Estimation

## Model specification

- Level equation: 4 lags level; 2 lags volatility
- Volatility equation: 2 lags level; 1 lag volatility


## Data

- GDP growth, BAA 10-Year Spreads - 1947:Q2 - 2019:Q4


## Estimation

- Use 1947:Q2 - 1953:Q1 as pre-sample to calibrate prior distributions
- 150,000 draws (50,000 burn-in)


## Understanding the Conditional Distribution

- We can write the conditional distribution as:

$$
\begin{aligned}
p\left(z_{t+1: t+f} \mid z^{t}\right)= & \int_{\Theta} \int_{H_{t}}\left[\int_{H_{t+1: t+f}} p\left(z_{t+1: t+f}, H_{t+1: t+f} \mid z^{t}, H_{t}, \Theta\right) d H_{t+1: t+f}\right] \\
& p\left(H_{t} \mid z^{T}, \Theta\right) p\left(\Theta \mid z^{T}\right) d H_{t} d \Theta
\end{aligned}
$$

Sources of uncertainty

- Future realizations of shocks
- Unobserved volatility states
- Parameters of the model
- These sources of uncertainty have implications for the overall uncertainty and tail behavior of the conditional distribution.


## Uncertainty and Tail Risk Impulse Responses

From the conditional distributions, we compute:

- $U I R_{f}\left[z_{i} \mid z^{t}, \nu_{j, t+1}^{*}\right]=\sqrt{\operatorname{Var}\left[z_{i, t+f} \mid z^{t}, \nu_{j, t+1}^{*}\right]}-\sqrt{\operatorname{Var}\left[z_{i, t+f} \mid z^{t}\right]}$ (Uncertainty Impulse Response)
- $S F I R_{f}\left[z_{i} \mid z^{t}, \nu_{j, t+1}^{*}\right]=S F_{f}\left[z_{i} \mid z^{t}, \nu_{j, t+1}^{*}\right]-S F_{f}\left[z_{i} \mid z^{t}\right]$ (Shortfall Impulse Response)
- $\operatorname{LRIR} R_{f}\left[z_{i} \mid z^{t}, \nu_{j, t+1}^{*}\right]=L R_{f}\left[z_{i} \mid z^{t}, \nu_{j, t+1}^{*}\right]-L R_{f}\left[z_{i} \mid z^{t}\right]$ (Longrise Impulse Response)

Uncertainty, shortfall, and longrise impulse responses integrate over the states $H^{t}$ and parameters $\Theta$.

## Identification Strategy

Sign and zero restrictions on the contemporaneous elasticities to identify macroeconomic and financial shocks...

$$
\begin{aligned}
z_{G D P, t} & =\underbrace{\eta_{12}}_{<0} z_{C S, t}+\underbrace{\eta_{13}}_{(-1 ; 1)} h_{G D P, t}+\underbrace{\eta_{14}}_{=0} h_{C S, t}+\nu_{M, t} \\
z_{C S, t} & =\underbrace{\eta_{21}}_{<0} z_{G D P, t}+\underbrace{\eta_{23}}_{(-0.5 ; 0.5)} h_{G D P, t}+\underbrace{\eta_{24}}_{=0} h_{C S, t}+\nu_{F, t} .
\end{aligned}
$$

- SR on Relationship between GDP growth and spreads.
- BR on Impact of GDP growth volatility on GDP growth and spreads.
- ZR on financial volatility.


## Identification Strategy (2)

... and macroeconomic and financial volatility shocks.

$$
\begin{aligned}
h_{G D P, t} & =\underbrace{\eta_{31}}_{<0} z_{G D P, t}+\underbrace{\eta_{32}}_{>0} z_{C S, t}+\underbrace{\eta_{34}}_{=0} h_{C S, t}+\nu_{M V, t}, \\
h_{C S, t} & =\eta_{41} z_{G D P, t}+\eta_{42} h_{G D P, t}+\eta_{43} h_{G D P, t}+\nu_{F V, t} .
\end{aligned}
$$

- SR on Endogenous component of GDP growth volatility.
- Separating financial and financial volatility shocks.


## Volatility of GDP Growth and Credit Spreads

GDP Growth Volatility


Credit Spread Volatility


- Estimation uncertainty is large for GDP growth volatility.
- Volatility is counter-cyclical.
- Strong evidence of rising volatility around recessions.


## Impulse Response Functions



- Both shocks generate business cycle correlations: GDP growth declines while corporate spreads and the volatility processes rise.
- Amplification from high volatility state is larger for financial shocks.
- Credible sets are wide and also get amplified by the volatility state.


## Credible Sets of Impulse Response Functions



- For all variables, the width of the credible set is of comparable size to the response itself.
- High volatility greatly amplifies uncertainty surrounding the effects of both shocks.


## Effects of Shocks on Uncertainty and Risk



- Relative impact of macro shocks is largest within the first year while financial shocks are more important at longer horizons.
- The tails capturing adverse risks move by more than the tails measuring upside risk.


## Decomposing the Channels of Transmission

## Volatility Channel





- Keeping the volatility of GDP growth innovations fixed lowers GDP growth uncertainty.
- Keeping the volatility of spread innovations fixed lowers both GDP growth and credit spread uncertainty.


## Concluding Remarks

- We analyze uncertainty and tail risk around economic and financial forecasts using a SV-VAR model estimated with Bayesian methods.
- Identified macro and financial shocks by imposing sign and zero restrictions.
- Macro shocks have significant impact on uncertainty and downside risk at shorter horizons, while financial shocks account for most of the variation at longer horizons.

APPENDIX

## Univariate SV-VAR Model

Level equation

$$
\begin{gathered}
z_{t}=c+\beta z_{t-1}+b_{1} \tilde{h}_{t-1}+H_{t}^{1 / 2} e_{t} \\
H_{t}=\exp \left(\tilde{h}_{t}\right)
\end{gathered}
$$

Volatility equation

$$
\tilde{h}_{t}=\alpha+\theta \tilde{h}_{t-1}+d_{1} z_{t-1}+S^{1 / 2} \eta_{t}
$$

Covariance structure

$$
\binom{e_{t}}{\eta_{t}} \sim N(0, \Sigma) ; \quad \Sigma=\left(\begin{array}{cc}
1 & \zeta \\
\zeta & 1
\end{array}\right)
$$

## Univariate SV-VAR Model

Homoskedastic VAR

$$
\begin{aligned}
& z_{t}=c+\beta z_{t-1}+\exp \left(\frac{1}{2} \alpha\right) e_{t} \\
& e_{t} \sim N(0,1)
\end{aligned}
$$



- Shifts in mean generate time variation in expected shortfall...
- But expected shortfall and longrise shift in lockstep.
- No time variation in variance.


## Univariate SV-VAR Model

## SV with no Feedback

$$
\begin{aligned}
z_{t} & =c+H_{t}^{1 / 2} e_{t}, \quad H_{t}=\exp \left(\tilde{h}_{t}\right) \\
\tilde{h}_{t} & =\alpha+\theta \tilde{h}_{t-1}+S^{1 / 2} \eta_{t} \\
\binom{e_{t}}{\eta_{t}} & \sim N\left(\binom{0}{0},\left(\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right)\right)
\end{aligned}
$$

Shift in Variance with No Feedback


- Shifts in variance generate time variation in expected shortfall...
- But expected shortfall and longrise move symmetrically.
- $e_{t}$ and $\eta_{t}$ shift mean and variance independently.


## Univariate SV-VAR Model

## Full SV Model

$$
\begin{aligned}
z_{t} & =c+\beta z_{t-1}+b_{1} \tilde{h}_{t-1}+H_{t}^{1 / 2} e_{t}, H_{t}=\exp \left(\tilde{h}_{t}\right) \\
\tilde{h}_{t} & =\alpha+\theta \tilde{h}_{t-1}+d_{1} z_{t-1}+S^{1 / 2} \eta_{t} \\
\binom{e_{t}}{\eta_{t}} & \sim N\left(\binom{0}{0},\left(\begin{array}{ll}
1 & \zeta \\
\zeta & 1
\end{array}\right)\right)
\end{aligned}
$$



- Shifts in mean and variance generate asymmetric time variation in shortfall and longrise.
- $e_{t}$ and $\eta_{t}$ can shift both mean and variance.


## Definition of Risk similar to ABG



- Downside risk: $S F=E\left[z \mid z<q_{\alpha}(z)\right]$ (Expected shortfall)
- Upside risk: $L R=E\left[z \mid z>q_{1-\alpha}(z)\right]$ (Expected longrise)


## Decomposing the Channels of Transmission

## Estimation Uncertainty Channel



- Importance of estimation uncertainty is largest at short horizons, when shocks have their largest effects.


## Decomposing the Channels of Transmission

## Higher-Order Channel





- Example: Credit spreads are positively correlated with credit spread volatility.
- A shock jumping off from a baseline of low credit spreads has smaller effects relative a shock from a baseline of high credit spreads.


## Asymmetric Effects of Bad Versus Good Shocks



- Shocks that move log volatility symmetrically have asymmetric effects on uncertainty.
- Estimation uncertainty increases overall uncertainty no matter whether the shock is positive or negative.


## Additional Results and Validation

## Comparison with other Time Series Measures of Uncertainty and Risk






## Additional Results and Validation

## Alternative Identification Scheme










- We employ an alternative identification scheme that assumes financial shocks are mediated through financial volatility instead of credit spreads.

